

MTH501 Midterm Solved Paper 2008 - Linear Algebra

MTH501 - Midterm Solved Paper of Linear Algebra - Year 2008

MIDTERM EXAMINATION

Fall 2008 (Session - 2)

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Time: 60 min

M = Marks= 38

MTH501 - Linear Algebra - Q. No. 1 (M - 1)

If A is a 2×2 matrix, the area of the parallelogram determined by the columns of A is

► A^{-1}

► $\det A$

► $\text{adj } A$

MTH501 - Linear Algebra - Q. No. 2 (M - 1)

Cramer's rule leads easily to a general formula for

► the inverse of an $n \times n$ matrix A

► the adjugate of an $n \times n$ matrix A

► the determinant of an $n \times n$ matrix A

MTH501 - Linear Algebra - Q. No. 3 (M - 1)

The transpose of an upper triangular matrix is

► lower triangular matrix

► upper triangular matrix

► diagonal matrix

MTH501 - Linear Algebra - Q. No. 4 (M - 1)

Let A be a square matrix of order 3×3 with $\det(A) = 21$, then $\det(2A) =$

► 168

► 186

► 21

► 126

MTH501 - Linear Algebra - Q. No. 5 (M - 1)

A basis is a linearly independent set that is as large as possible. (<http://www.vuzs.info/old-papers.html>)

► True

► False

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MTH501 - Linear Algebra - Q. No. 6 (M - 1)

Col A is all of 0^m if and only if

► the equation $Ax = 0$ has a solution for each b in 0^m

► the equation $Ax=b$ has a solution for each b in 0^m

► the equation $Ax=b$ has a solution for a fixed b in 0^m .

MTH501 - Linear Algebra - Q. No. 7 (M - 1)

$$A = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \quad B = \begin{bmatrix} B_1 \\ B_2 \end{bmatrix}$$

If and, then the partitions of A and B

► are not conformable for block multiplication

► **are conformable for AB block multiplication**

► are not conformable for BA block multiplication

MTH501 - Linear Algebra - Q. No. 8 (M - 1)

Two vectors are linearly dependent if and only if they lie

► on a line parallel to x-axis

► on a line through origin

► on a line parallel to y-axis

MTH501 - Linear Algebra - Q. No. 9 (M - 1)

The equation $x = p + t v$ describes a line

► through v parallel to p

► through p parallel to v

► through origin parallel to p

MTH501 - Linear Algebra - Q. No. 10 (M - 1)

Let A be an $m \times n$ matrix. If for each b in \mathbb{R}^m the equation $Ax=b$ has a solution then

► A has pivot position in only one row

► Columns of A span \mathbb{R}^m

► Rows of A span \mathbb{R}^m

MTH501 - Linear Algebra - Q. No. 11 (M - 1)

$$x_1 - 2x_2 + x_3 = 8$$

$$2x_2 + 7x_3 = 0$$

$$-4x_1 + 3x_2 + 9x_3 = -6$$

Given the system the augmented matrix for the system is

$$\begin{bmatrix} 1 & -2 & 1 & 8 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 2 & -7 & -8 \end{bmatrix}$$

$$\begin{bmatrix} -4 & 3 & 9 & -6 \end{bmatrix}$$

► $\begin{bmatrix} 1 & -2 & 1 & 0 \end{bmatrix}$

$$\begin{bmatrix} 0 & 2 & -7 & 8 \end{bmatrix}$$

$$\begin{bmatrix} -4 & 3 & 9 & -6 \end{bmatrix}$$

► $\begin{bmatrix} 1 & -2 & 1 & \end{bmatrix}$

$$\begin{vmatrix} 0 & 2 & -8 \end{vmatrix}$$

$$\begin{vmatrix} -4 & 5 & 9 \end{vmatrix}$$

► $\begin{vmatrix} 1 & -2 & 1 & 8 \end{vmatrix}$

$$\begin{vmatrix} 0 & 2 & -7 & 0 \end{vmatrix}$$

$$\begin{vmatrix} -4 & 3 & 9 & -6 \end{vmatrix}$$
 (<http://www.vuzs.info/old-papers.html>)

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MTH501 - Linear Algebra - Q. No. 12 (M - 1)

$$\begin{vmatrix} 1 & 2 & 0 \end{vmatrix}$$

$$\begin{vmatrix} 0 & 1 & 0 \end{vmatrix}$$

$$\begin{vmatrix} 1 & 0 & 0 \end{vmatrix}$$

Consider the linear transformation T such that

$$\begin{vmatrix} 1 & 2 & 0 \end{vmatrix}$$

$$\begin{vmatrix} 0 & 1 & 0 \end{vmatrix}$$

$$\begin{vmatrix} 1 & 0 & 0 \end{vmatrix}$$

is the matrix of linear transformation then T

$$\begin{vmatrix} 2 \end{vmatrix}$$

$$\begin{vmatrix} 4 \end{vmatrix}$$

$$\begin{vmatrix} 6 \end{vmatrix}$$

is

$$\begin{vmatrix} 10 \end{vmatrix}$$

$$\begin{vmatrix} 4 \end{vmatrix}$$

$$\begin{vmatrix} 2 \end{vmatrix}$$

► $\begin{vmatrix} 1 \end{vmatrix}$

$$\begin{vmatrix} 0 \end{vmatrix}$$

$$\begin{vmatrix} 9 \end{vmatrix}$$

► $\begin{vmatrix} 10 \end{vmatrix}$

$$\begin{vmatrix} 4 \end{vmatrix}$$

$$\begin{vmatrix} 1 \end{vmatrix}$$

► $\begin{vmatrix} 1 \end{vmatrix}$

|2|

|3|

|2|

MTH501 - Linear Algebra - Q. No. 13 (M - 1)

$$\begin{vmatrix} a & b & c \\ d & e & f \end{vmatrix} = 5 \quad \begin{vmatrix} a & b & c \\ 3d & 3e & 3f \end{vmatrix}$$

If $\begin{vmatrix} g & h & i \end{vmatrix}$ then $\begin{vmatrix} g & h & i \end{vmatrix}$ will be

► 15

► **45**

► 135

► 60

MTH501 - Linear Algebra - Q. No. 14 (M - 1)

For an $n \times n$ matrix $(A^t)^t =$

► A^t

► **A**

► A^{-1}

► $(A^{-1})^{-1}$

MTH501 - Linear Algebra - Q. No. 15 (M - 1)

Each Linear Transformation T from R^n to R^m is equivalent to multiplication by a matrix A of order

► $m \times n$

► **$n \times m$**

► $n \times n$

► $m \times m$

MTH501 - Linear Algebra - Q. No. 16 (M - 1)

Reduced echelon form of the matrix $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \end{bmatrix}$ is

► $\begin{bmatrix} 1 & 2 & 3 \\ 0 & 0 & 1 \end{bmatrix}$

► $\begin{bmatrix} 1 & 0 & 3 \\ 0 & 0 & 1 \end{bmatrix}$

► $\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -2 \end{bmatrix}$

► $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \end{bmatrix}$

MTH501 - Linear Algebra - Q. No. 17 (M - 2)

Find vector and parametric equations of the plane that passes through the origin of \mathbf{R}^3 and is parallel to the vectors $\mathbf{v}_1 = (1, 2, 5)$ and $\mathbf{v}_2 = (5, 0, 4)$.

MTH501 - Linear Algebra - Q. No. 18 (M - 2)

Which of the following is true? If V is a vector space over the field F .(justify your answer)

- (a) $\{x + y / x \in V, y \in V\} = V$
- (b) $\{x + y / x \in V, y \in V\} = V \times V$
- (c) $\{\lambda v / v \in V, \lambda \in F\} = F \times V$

MTH501 - Linear Algebra - Q. No. 19 (M - 3)

Let

$v_1 = \begin{bmatrix} 1 \\ 0 \\ -2 \end{bmatrix}$, $v_2 = \begin{bmatrix} -2 \\ 1 \\ 7 \end{bmatrix}$, and $y = \begin{bmatrix} h \\ -3 \\ -5 \end{bmatrix}$

For what value(s) of h is y in the plane generated by v_1 and v_2 ?

MTH501 - Linear Algebra - Q. No. 20 (M - 5)

With T defined by $T(x) = Ax$, find a vector x whose image under T is b , and determine whether x is unique. vuzs

$$A = \begin{bmatrix} 1 & -5 & -7 \\ -3 & 7 & 5 \end{bmatrix}, \quad b = \begin{bmatrix} -2 \\ -2 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & -5 & -7 \\ -3 & 7 & 5 \end{bmatrix}, \quad b = \begin{bmatrix} -2 \\ -2 \end{bmatrix}$$

MTH501 - Linear Algebra - Q. No. 21 (M - 10)

Given A and b , write the augmented matrix for the linear system that corresponds to the matrix equation $Ax = b$. Then solve the system and write the solution as a vector. (<http://www.vuzs.info/old-papers.html>)

$$A = \begin{bmatrix} 1 & 2 & 1 \\ -3 & -1 & 2 \\ 0 & 5 & 3 \end{bmatrix}, \quad b = \begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix}$$

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